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PAPER

Visco-thermal effects in acoustic metamaterials: from total transmission to total reflection and high absorption

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Keywords: acoustic metamaterials, viscous and thermal losses, extraordinary transmission, Fabry–Perot resonance

Abstract

We theoretically and experimentally investigate visco–thermal effects on the acoustic propagation through metamaterials consisting of rigid slabs with subwavelength slits embedded in air. We demonstrate that this unavoidable loss mechanism is not merely a refinement, but that it plays a dominant role in the actual acoustic response of the structure. Specifically, in the case of very narrow slits, the visco–thermal losses avoid completely the excitation of Fabry–Perot resonances, leading to 100% reflection. This is exactly opposite to the perfect transmission predicted in the idealised lossless case. Moreover, for a wide range of geometrical parameters, there exists an optimum slit width at which the energy dissipated in the structure can be as high as 50%. This work provides a clear evidence that visco–thermal effects are necessary to describe realistically the acoustic response of locally resonant metamaterials.

1. Introduction

Metamaterials are artificial structured materials in which the presence of resonances in the micro/meso-scale leads to unprecedented properties [1, 2]. In recent years, metamaterials consisting of rigid slabs with subwavelength perforations have attracted considerable attention due to their ability to achieve normalised-to-area transmission (i.e., transmission normalised to the fraction of area occupied by the holes) significantly bigger than unity, a phenomenon known as extraordinary acoustic transmission (EAT) [3]. This phenomenon, analogue to extraordinary optical transmission [4], can be achieved by means of different physical mechanisms, such as the excitation of Fabry–Perot (FP) resonances in the holes [3, 5–7], the acoustic Brewster angle [8, 9], or the acoustic analog to the supercoupling effect in density–near–zero metamaterials [10]. Promising applications to this fascinating phenomenon have been suggested, including acoustic collimators [11], superlenses [12], highly efficient Fresnel lenses [13], beam shifters [14], passive phased arrays [15] and invisibility cloaks [16].

A main limitation in the practical realization of EAT and other unconventional phenomena in locally resonant metamaterials arises from the unavoidable presence of viscous and thermal boundary layers at the solid–fluid interface [17, 18], which can induce important losses. However, only a few papers have investigated boundary layer effects in metamaterials. In [19], it was demonstrated that visco–thermal dissipation has a strong influence in the slow sound propagation in waveguides with side resonators, hindering the formation of near–zero group velocity dispersion bands. This feature was exploited later to design low frequency acoustic absorbers [20]. More recently, visco–thermal dissipation in microslits has been used to enhance the attenuation of metamaterials [21], and important boundary layer effects have also been reported in phononic crystals [22, 23].

The goal of the present work is to investigate visco–thermal losses in acoustic metamaterials consisting of rigid slabs with subwavelength slits. Previous studies have already proven that this dissipation mechanism may significantly attenuate the otherwise perfect transmission peaks associated to FP resonances [8, 24], while the nonresonant EAT mechanism based on the Brewster angle remains much less affected [8]. However, these works lack a clear theoretical analysis of the behaviour of the system in the presence of losses and do not describe completely the physical mechanisms governing the reduction of transmission, in relation to reflection and/or dissipation. This paper complements these earlier studies, providing an experimental and theoretical analysis of the acoustic transmission, reflection, and absorption in the presence of visco–thermal dissipation. Our results

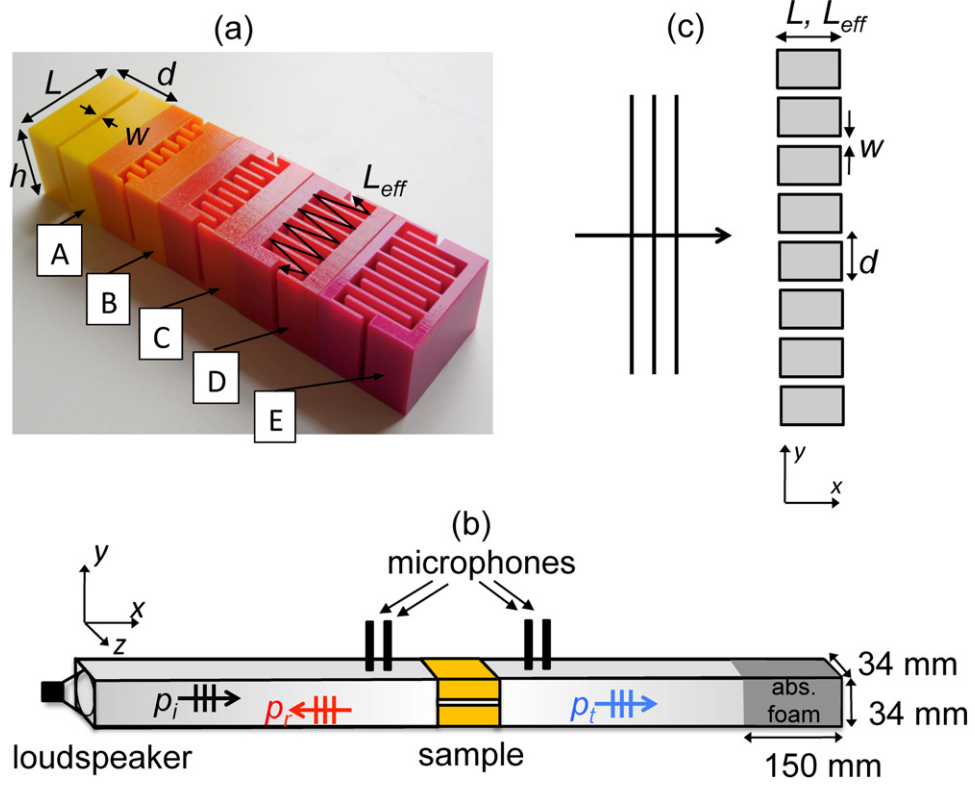


Figure 1. (a) Samples under test, characterised by the slit width $w = 2.7$ mm, the grating period $d = 34$ mm and the effective grating thickness $L_{eff} = L = 52$ mm for Sample A, $L_{eff} = 2.08L$ for Sample B, $L_{eff} = 3.16L$ for Sample C, $L_{eff} = 4.24L$ for Sample D and $L_{eff} = 5.32L$. The cover of the samples has been removed to reveal the internal structure. (b) Schematic of the experimental setup. (c) 2D perforated slab equivalent to the one studied experimentally.

demonstrate that this loss mechanism avoids completely the excitation of Fabry–Perot resonances in gratings with very narrow slits, which leads to 100% reflection. In addition, we prove that the optimum absorption is about 50%, which is attributed to the critical coupling of the slit cavity resonators with the host medium [25–28].

2. Experimental setup

Figure 1(a) shows the samples under experimental consideration, which were fabricated using 3D printing (Stratasys Objet500). The material used was a rigid thermoplastic (Vero materials (c)) with manufacturer specified mass density $1.17\text{--}1.18\text{ g cm}^{-3}$ and modulus of elasticity 2–3 GPa. The samples are rectangular blocks with an air channel connecting the input and output sides. Sample A has a straight channel, while in samples B to E the channels describe a zigzag path. For wavelengths much bigger than the height of the corrugations, the zigzag channel behaves similarly to a straight slit with effective length L_{eff} , which is approximately equal to shortest path taken by the wave to pass through the structure [29, 30]. The samples were placed between two aluminium tubes with square cross-section and 34 mm inner side, as shown in figure 1(b). The square cross-section artificially imposes periodic boundary conditions in the transverse directions. Since, from the point of view of the plane waves traveling inside the tubes, the samples' geometry is constant along the z -direction, no momentum can be excited in this direction. Therefore, the pressure field is always constant in z , meaning that the structure is equivalent to a 2D slab with a periodic array of slits along the y -direction, see figure 1(c). The relevant geometrical parameters of this equivalent system are the slit width $w = 2.7$ mm, the grating period $d = 34$ mm and the effective grating thickness L_{eff} . $L_{eff} = L = 52$ mm for Sample A, $L_{eff} = 2.08L$ for Sample B, $L_{eff} = 3.16L$ for Sample C, $L_{eff} = 4.24L$ for Sample D and $L_{eff} = 5.32L$ for Sample E. The transmission $T = |p_t/p_i|^2$, reflection $R = |p_r/p_i|^2$, and absorption coefficient $A = 1 - R - T$ were measured with 4 microphones (G.R.A.S. 40BD) using the two-port technique [31], where p_i , p_r and p_t are respectively the complex amplitude of the incident, reflected and transmitted plane mode [see figure 1(b)]. We measured these quantities using phase sensitive detection with a sinusoidal wave as reference signal, injected to a loudspeaker (Clarion SRE 212 H) on the left extremity. A 150 mm thick absorbing foam was placed on the right side to minimise backward reflections. The testing frequency range was limited to $[1 - 5]$ kHz. The lower limit is imposed by the loudspeaker, which is not able to radiate sound below approximately 1 kHz. The upper limit is

imposed by the cutoff frequency of the first high-order mode in the ducts, approximately 5 kHz, so that only the plane mode excites the samples.

3. Model

The acoustic propagation through the grating depicted in figure 1(c) is modelled using a multimodal approach developed in previous works by the authors [13, 32]. We express the acoustic pressure field, $p(x, y)$, as a modal decomposition,

$$p(x, y) = \sum_n (A_n e^{j\beta_n x} + B_n e^{-j\beta_n x}) \phi_n(y), \quad (1)$$

where A_n and B_n are respectively the modal amplitude of the n -th forward and backward mode, β_n are the propagation constants, and $\phi_n(y)$ are the eigenfunctions. In the surrounding space with periodic boundary conditions, the eigenfunctions are

$$\phi_n(y) = \frac{1}{\sqrt{d}} e^{j[2n\pi/d + k \sin(\theta)]y}, \quad n \in \mathbb{Z}, \quad (2)$$

where $k = \omega/c$ is the wavenumber in free space, ω is the angular frequency, c is the sound speed, and θ is the incidence angle with respect to x of the impinging plane wave (here $\theta = 0$). Assuming rigid boundaries, the eigenmodes of the slit are given by,

$$\phi_n(y) = \sqrt{\frac{2 - \delta_{n,0}}{w}} \cos\left[\frac{n\pi}{w}\left(y - \frac{w}{2}\right)\right], \quad n \in \mathbb{N} \quad (3)$$

with $\delta_{n,0}$ the Kronecker delta ($\delta_{n,0} = 1$ for $n = 0$ and $\delta_{n,0} = 0$ otherwise).

In the absence of losses, the propagation constants of the slit modes are given by the dispersion relation $\beta_n^2 = k^2 - (n\pi/w)^2$. The effect of the viscous and thermal losses can be taken into account by introducing an additional term into these propagation constants (see [33]),

$$\beta_n^2 = k^2 - \left(\frac{n\pi}{w}\right)^2 + \frac{2k}{w}(2 - \delta_{n,0})(\text{Im}\{\varepsilon_n\} - j \text{Re}\{\varepsilon_n\}) \quad (4)$$

where

$$\varepsilon_n = \left[1 - \left(\frac{n\pi}{wk}\right)^2\right] \varepsilon_v + \varepsilon_t, \quad (5)$$

$$\varepsilon_v = (1 + j) \sqrt{\frac{kl_v}{2}}, \quad (6)$$

and

$$\varepsilon_t = \frac{(1 + j)}{(\gamma - 1)} \sqrt{\frac{kl_t}{2}}, \quad (7)$$

In equations (5)–(7), $\gamma = 1.4$ the adiabatic specific heat ratio of air, l_v is the viscous characteristic length and l_t is the thermal characteristic length. At standard conditions, $c \approx 344$ m/s, l_v and l_t are respectively $l_v = 4.5 \times 10^{-8}$ m and $l_t = 6.2 \times 10^{-8}$ m (see [33]). We note that, according to the time convention chosen in this paper ($e^{-j\omega t}$), we only keep solutions to equation (4) fulfilling $\text{Re}\{\beta_n\}, \text{Im}\{\beta_n\} \geq 0$.

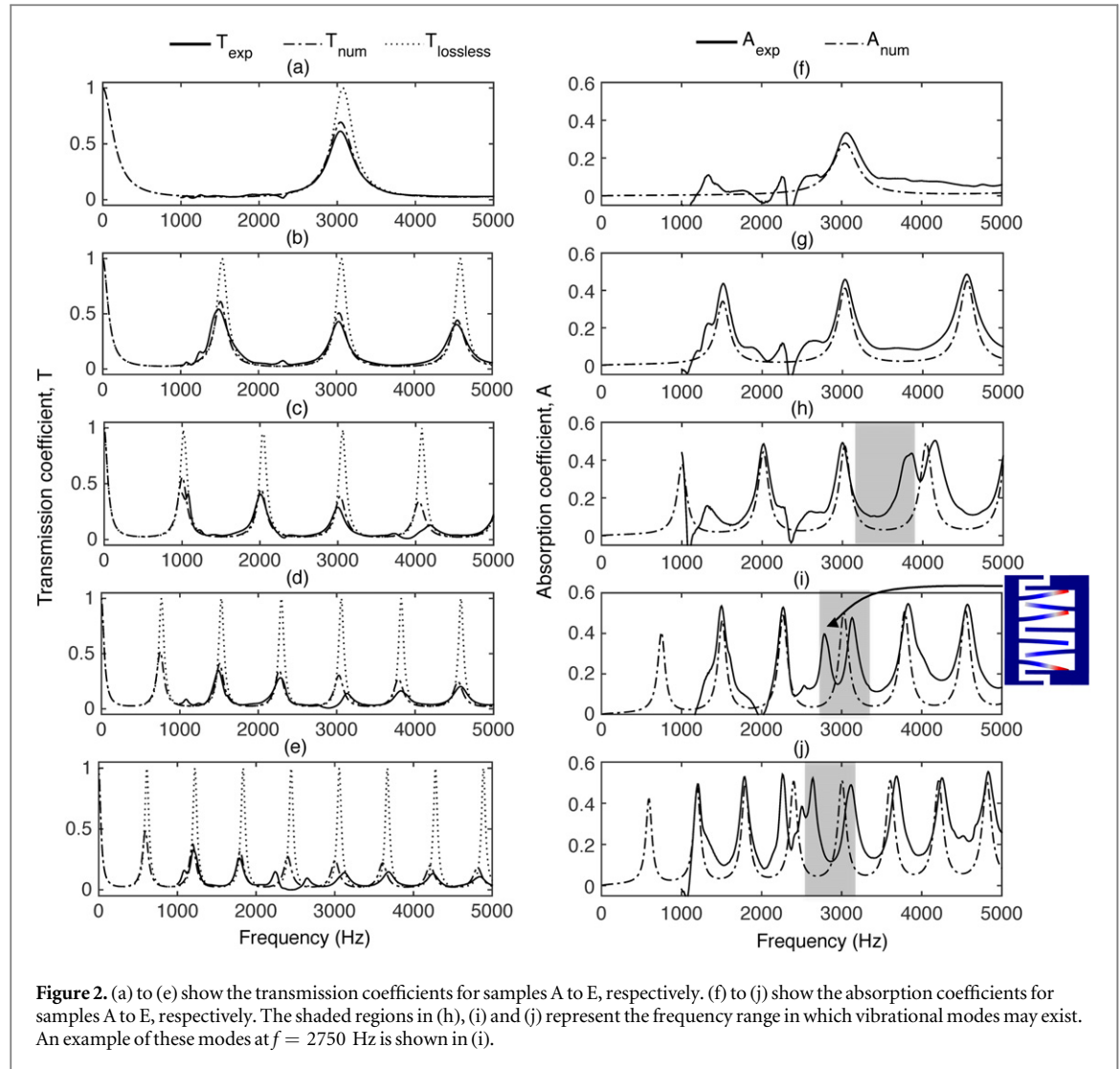
Writing the continuity equations of pressure and normal velocity at the interface between the grating and the surrounding space leads to the reflection and transmission matrices, \mathbf{R} and \mathbf{T} (see [13, 32] for details), defined as $\vec{A}_R = \mathbf{R}\vec{A}_I$ and $\vec{A}_T = \mathbf{T}\vec{A}_I$, where \vec{A}_I , \vec{A}_R and \vec{A}_T are row vectors containing the incident, reflected and transmitted modal amplitudes. Finally, the energy reflection, transmission and absorption coefficients are given respectively by

$$R = \frac{\text{Re}\{\vec{A}_R^t (\mathbf{Y}\vec{A}_R)^*\}}{\text{Re}\{\vec{A}_I^t (\mathbf{Y}\vec{A}_I)^*\}}, \quad (8)$$

$$T = \frac{\text{Re}\{\vec{A}_T^t (\mathbf{Y}\vec{A}_T)^*\}}{\text{Re}\{\vec{A}_I^t (\mathbf{Y}\vec{A}_I)^*\}}, \quad (9)$$

$$A = 1 - R - T, \quad (10)$$

where $\mathbf{Y} = \text{diag}\{\beta_n/\rho ck\}$ and superscripts 't' and '*' indicate respectively the transpose and the complex conjugate. The series of equation (1) was truncated to 40 modes in the free, periodic space and 5 modes in the slit, from which only the fundamental one [$n = 0$ in equations (2)–(4)] is propagative.



4. Results

We start our analysis by studying the influence of L_{eff} in the acoustic response of the samples. Figures 2(a)–(e) show the experimental (solid lines) and numerical (dash-dotted lines) transmission coefficients. The lossless transmission coefficients (dotted lines), obtained by replacing β_n with $\beta_n^2 = k^2 - (n\pi/w)^2$ in equation (4), are also shown. The lossless transmission coefficients exhibits the perfect transmission peaks typical of FP resonances at $f \approx sc/2L_{eff}$, with s a positive integer. However, when visco–thermal effects are included in the model, we observe a strong attenuation of the resonance peaks as L_{eff} increases, which is in good agreement with the experimental results. We also observe a downshift of the resonance frequencies compared to the lossless case, due to the slowing down of the wave because of the dissipation [24]. These figures represent a first and clear evidence that neglecting visco–thermal effects leads to a poor description of the actual metamaterial response.

Figures 2(f)–(j) show the absorption coefficients as a function of frequency for the different samples. Experimental and numerical results are in good qualitative agreement and demonstrate a strong dissipation at the FP resonance frequencies. The attenuation peaks reach between 33% and 55% in experiments, and between 30% and 50% in the numerical results. We also notice an increase of absorption with frequency, which is due to the fact that $\text{Im}\{\beta_0\}$ (β_0 is the propagation constant of the fundamental slit mode) also increases with frequency, approximately as \sqrt{f} , see equation (4).

Although the agreement between experimental and numerical results is globally good, particularly in terms of the amplitude of the absorption peaks, we also observe some discrepancies. The experimental absorption coefficient is in general higher than the numerical one, which can be attributed to additional losses in the experimental setup, as visco–thermal losses in the aluminium tubes (these effects are only modelled within the slits), material losses, or losses due to energy leakage between the different pieces forming the experimental apparatus. We also observe features in the experimental curves that are not observed in the numerical results.

The experimental curves around the fourth peak in figures 2(h)–(j) exhibit an additional peak, not observed in the numerical curve. The origin of these peaks is the excitation of vibrational modes of the samples, which is consistent with the downshift of the peak frequencies as the height of the internal corrugations increases. We verified this through the computation of the samples' vibrational modes using Comsol Multiphysics. The shaded regions in figures 2(h)–(j) represent the frequency range in which vibrational modes were obtained, accordingly to the range of mechanical parameters provided by the manufacturer. An example of these modes at $f = 2750$ Hz is displayed in figure 2(i).

It is remarkable to achieve such high absorption using visco–thermal effects, considering that the slit width is about 2 orders of magnitude bigger than the viscous and thermal boundary layers ($\sim 10^{-5}$ m [34]). This behaviour, which is consistent with recent observations by Ward *et al.* [24], is rather surprising as intuition suggest that visco–thermal effects would only become relevant when the slit width is of the same order as the boundary layers' thickness.

To quantify the maximum amount of energy that can be absorbed in these structures by the combination of FP resonances and visco–thermal losses, we have computed the amplitude of the first absorption peak, A_{res} , as a function of the geometrical parameters. Figure 3(a) shows A_{res} versus L_{eff} and w for $d = 34$ mm fixed, and figure 3(d) shows the same quantity versus d and w for $L_{eff} = 52$ mm fixed. We observe that the parameter having a stronger influence on the response is the slit width w . For any L_{eff} and d considered, A_{eff} exhibits a maximum between $w = 0.5$ mm and $w = 2$ mm, at which the structure dissipates about 50% of the incident energy.

The vanishing of A_{res} after its maximum is due to the fact that the acoustic impedance of the surrounding media, $Z_1 = \rho c/d$, approaches that of the slit cavity, $Z_2 = \rho ck/w\beta_0$, as $w \rightarrow d$. This inhibits the formation of a high amplitude standing wave in the slit cavity and reduces the ability to dissipate energy. However, the vanishing of A_{res} as $w \rightarrow 0$ is less straightforward. In principle, visco–thermal losses (given by $\text{Im}\{\beta_0\}$) and the strength of the FP resonance (provided by the impedance ratio Z_1/Z_2) increase as $w \rightarrow 0$ when considered separately. Hence, one should expect the dissipation to increase also in this region. However, inspecting the transmission and reflection coefficients at resonance, respectively T_{res} [figures 3(b) and 3(e)] and R_{res} [figures 3(c) and 3(f)], we observe that the structure behaves as a perfect reflector as $w \rightarrow 0$, meaning that very little energy is stored (and therefore dissipated) in the resonator. Remarkably, although the dramatic drop in the transmission is a direct consequence of the presence of losses in the system, this drop is not reflected in an increase of dissipation.

To explain this counterintuitive behaviour, we derive analytical expressions for the reflection and transmission coefficients. To accomplish this, we reduce our model to only the fundamental mode in both the slit cavity and the free, periodic space [$n = 0$ in equation (1)]. The amplitude reflection and transmission coefficients of this mode, respectively r_0 and t_0 , take the following form

$$r_0 = \frac{\left(1 - \frac{Z_1^2}{Z_2^2}\right)(e^{-2j\beta_0 L_{eff}} - 1)}{\left(\frac{Z_1}{Z_2} + 1\right)^2 e^{-2j\beta_0 L_{eff}} - \left(\frac{Z_1}{Z_2} - 1\right)^2} \quad (11)$$

and

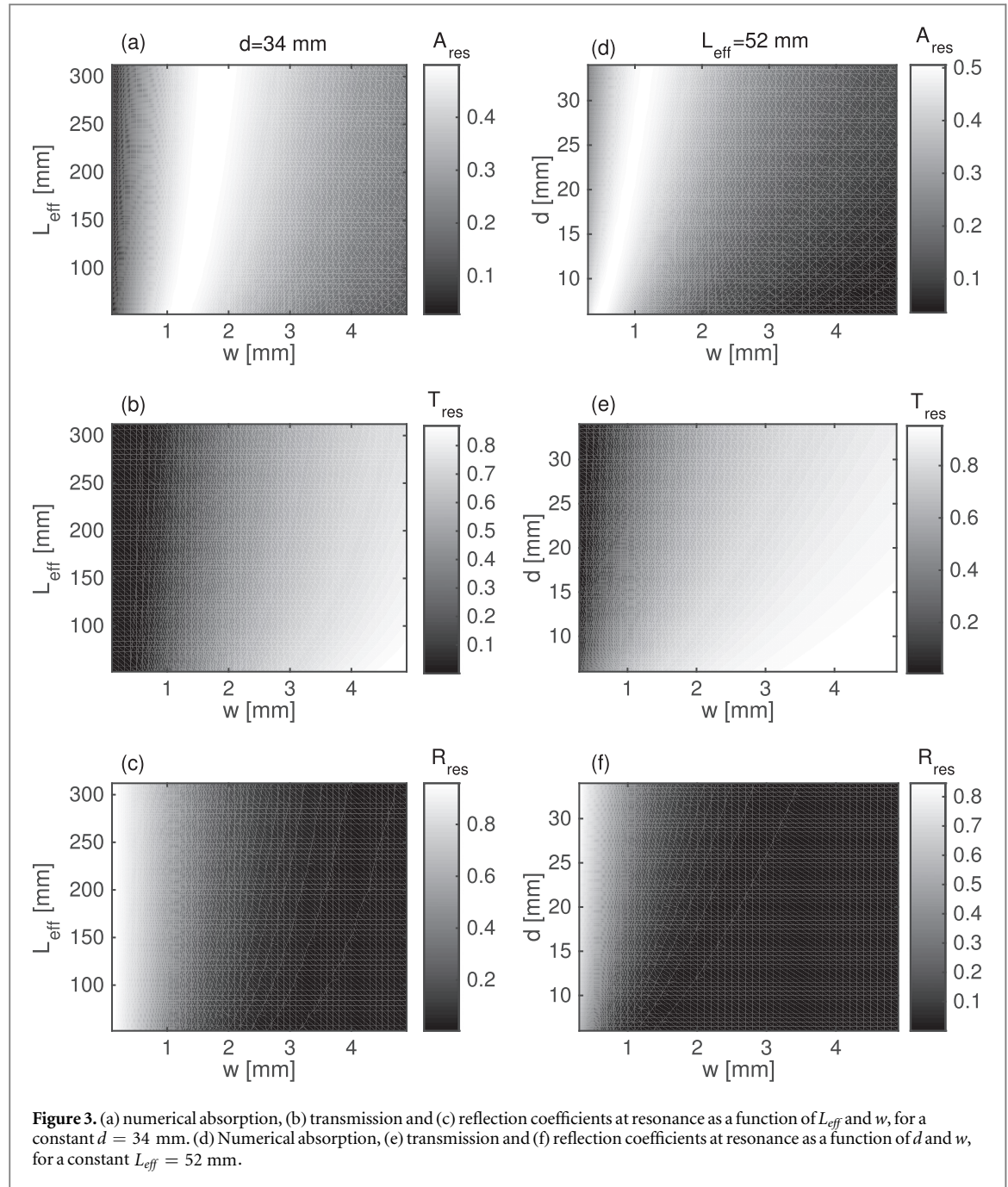
$$t_0 = \frac{4\frac{Z_1}{Z_2}e^{j\beta_0 L_{eff}}}{\left(1 + \frac{Z_1}{Z_2}\right)^2 - \left(\frac{Z_1}{Z_2} - 1\right)^2 e^{2j\beta_0 L_{eff}}}, \quad (12)$$

from which R and T are obtained as $R = |r_0|^2$ and $T = |t_0|^2$. In the absence of losses ($\beta_0 = k$) the FP resonances appear when $e^{2j\beta_0 L_{eff}} = 1$, or equivalently when $k = s\pi/L_{eff}$, which leads to $R = 0$ and $T = 1$, regardless of L_{eff} , w , and d [3, 5–7, 30]. However, when visco–thermal losses are accounted for, β_0 is $\beta_0 = \text{Re}\{\beta_0\} + j\text{Im}\{\beta_0\}$, and FP resonances appear when $e^{2j\text{Re}\{\beta_0\}L_{eff}} = 1$. In such case, the reflection and transmission coefficients become

$$r_{0,res} = \frac{\left(1 - \frac{Z_1^2}{Z_2^2}\right)(e^{2\text{Im}\{\beta_0\}L_{eff}} - 1)}{\left(\frac{Z_1}{Z_2} + 1\right)^2 e^{2\text{Im}\{\beta_0\}L_{eff}} - \left(\frac{Z_1}{Z_2} - 1\right)^2} \quad (13)$$

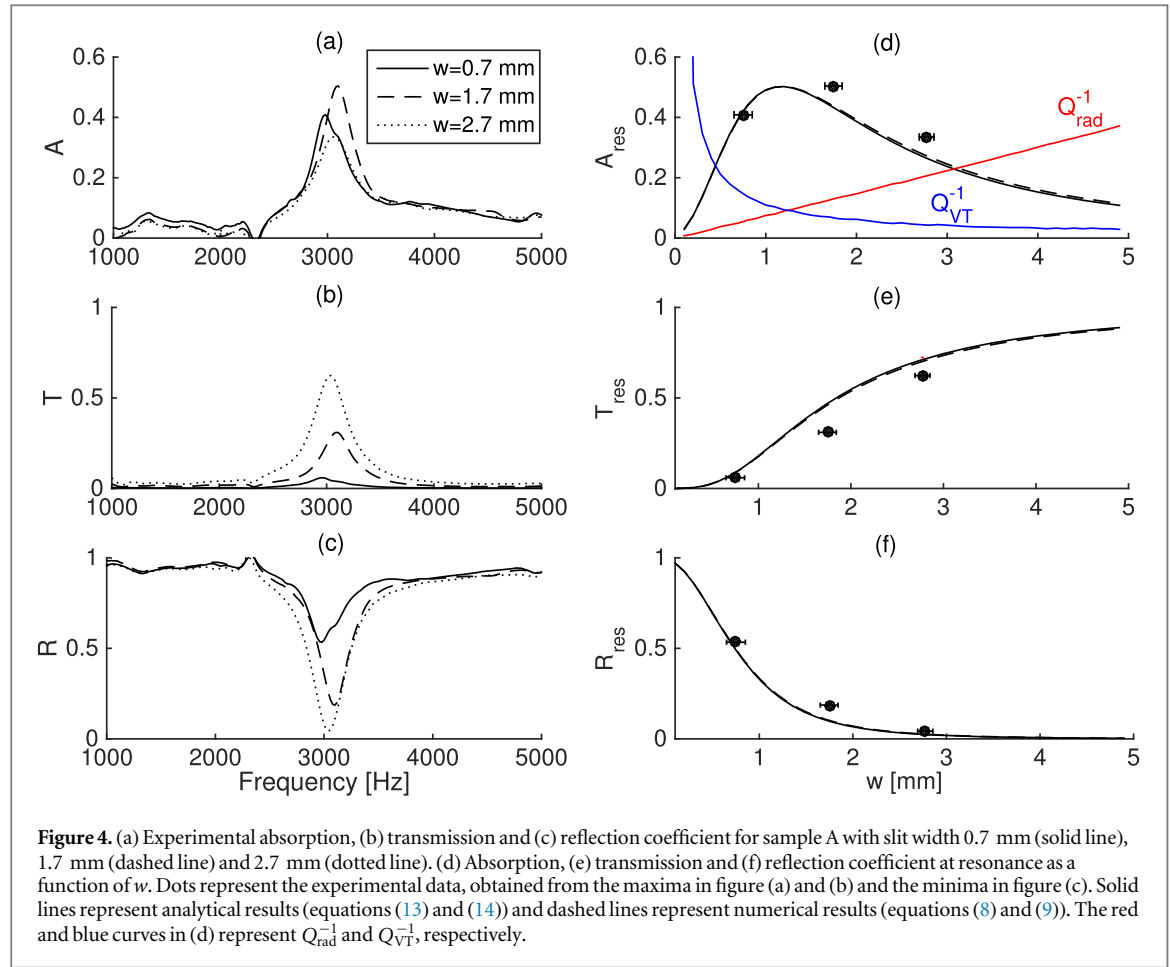
and

$$t_{0,res} = \frac{4\frac{Z_1}{Z_2}e^{-\text{Im}\{\beta_0\}L_{eff}}}{\left(1 + \frac{Z_1}{Z_2}\right)^2 - \left(\frac{Z_1}{Z_2} - 1\right)^2 e^{-2\text{Im}\{\beta_0\}L_{eff}}}. \quad (14)$$



Contrary to the conservative case (equations (11) and (12)), we see that the acoustic response at resonance depends on the geometrical parameters, both on L_{eff} and w/d (through the impedance ratio $Z_1/Z_2 \propto w/d$). For $w \ll d$, that is $Z_1/Z_2 \rightarrow 0$, one has $R \rightarrow 1$ and $T \rightarrow 0$, which is consistent with the numerical results in figure 3. Remarkably, this result holds for any $L_{\text{eff}} > 0$ as long as dissipation is present in the slit ($\text{Im}\{\beta_0\} > 0$), which is always true in realistic situations. In other words, the reflection always tends to 1 in slabs such that $w \ll d$, regardless of the thickness L_{eff} . This is visible in figure 3(c). Another implication of equations (13) and (14) is that, when w is very small (say $w < 1$ mm), high transmission can be achieved only if the period d is comparable to w , that is when $Z_1/Z_2 \rightarrow 1$. This means that EAT (i.e. transmission considerably bigger than unity when normalised to the ratio w/d) cannot be achieved in slabs with very narrow slits.

In order to obtain an experimental evidence for this behaviour we have fabricated and tested two additional samples. The new samples are identical to sample A, but the slit width is equal to 0.7 mm and 1.7 mm. Figure 4(a) to 4(c) show, respectively, the experimental absorption, transmission and reflection coefficients. These figures confirm the behaviour described previously in figure 3: the reflection (transmission) increases (decreases) monotonically as $w \rightarrow 0$, and there is an optimum w that maximises the absorption. For a quantitative comparison of experiments with theory, figures 4(d)–4(f) show, respectively, A_{res} , R_{res} and T_{res} as a function of w . Solid lines represent the analytical results obtained with equations (11) and (12). Dashed lines



represent the numerical result obtained with the multimodal method, equations (8) and (9). The experimental data, obtained from the maxima of A and T , or minima of R in figures 4(a)–(c) is represented with dots. Horizontal error bars in experimental results represent the standard deviation of the actual slit width from the desired values, measured at four different points along the slit. This deviation was less than 0.1 mm for all samples. The trend exhibited by experimental results agrees very well with both numerical and analytical results, either in absorption, transmission and reflection, which corroborates the theoretical predictions.

The optimum 0.5 absorption found in figures 3(a), 3(d) and 4(d) is a characteristic of systems with open resonators fulfilling the critical coupling condition [25], a phenomenon that has recently attracted considerable attention in acoustics [26–28]. This condition refers to the situation in which the energy dissipated in the resonator is equal to the energy radiated to the host medium. In the case of a symmetric resonator and one-sided excitation (as considered in this paper) critical coupling leads to 0.5 absorption [26–28]. To corroborate this phenomenon in our system, we use the quality factor of the Fabry–Perot transmission peaks, $Q = E/(\Delta E_{\text{VT}} + \Delta E_{\text{rad}})$, where E is the energy stored in the slit cavity resonator, ΔE_{VT} is the energy dissipated per cycle due to visco-thermal effects and ΔE_{rad} is the energy radiated per cycle. This quantity is computed as $Q = f_{\text{res}}/\Delta f$, where f_{res} is the resonance frequency and Δf is the half-power bandwidth. The quality factor can also be expressed as $Q^{-1} = Q_{\text{VT}}^{-1} + Q_{\text{rad}}^{-1}$, with $Q_{\text{VT}}^{-1} = \Delta E_{\text{VT}}/E$ and $Q_{\text{rad}}^{-1} = \Delta E_{\text{rad}}/E$. In the absence of visco-thermal losses ($Q_{\text{VT}}^{-1} = 0$) computing the quality factor of the system gives directly the term Q_{rad}^{-1} . Once Q_{rad}^{-1} is known, the term Q_{VT}^{-1} is given by $Q_{\text{VT}}^{-1} = Q^{-1} - Q_{\text{rad}}^{-1}$. Notice that critical coupling occurs when $Q_{\text{VT}}^{-1} = Q_{\text{rad}}^{-1}$. The red and blue curves in figure 4(d) represent, respectively, Q_{rad}^{-1} and Q_{VT}^{-1} . As expected, it is observed that the optimum 0.5 absorption ($w = 1.20$ mm) is very close to the crossing between Q_{rad}^{-1} and Q_{VT}^{-1} ($w = 1.24$ mm). It is interesting to note that critical coupling may lead to 100% absorption using a reflecting surface close to the slab [26, 27], or using asymmetric resonators [28]. These configurations provide an interesting approach for the development of high performance sound absorbing materials.

5. Conclusion

In summary, visco-thermal effects are essential to describe realistically the acoustic response of metamaterials composed of rigid slabs with subwavelength slits. Due to the presence of this loss mechanism, the behaviour of the structure at the FP resonances depends completely on the geometrical parameters, which can be adjusted to achieve high transmission, high absorption or high reflection. Our work may have important implications in the design of acoustic metamaterials. For instance, the inability to obtain sharp FP resonances in slabs with very narrow slits compromises the practical realization of resonant EAT at ultrasonic frequencies. On the other hand, understanding and exploiting this property gives the possibility to design subwavelength sized, tailorable devices providing high transmission, high reflection or high absorption. From a more general perspective, we expect that our work will result in widespread consideration of this unavoidable loss mechanism in acoustic metamaterials research.

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